

Pre-Calculus 12  
Rational Expression Review

Name: \_\_\_\_\_  
Block: \_\_\_\_\_

1. Add the following fractions.

a)  $\frac{1}{2} + \frac{2}{3}$

b)  $\frac{x}{y} + \frac{1}{xy}$

The same method can be applied when adding fractions involving trigonometric functions.

$$\frac{\sin \theta}{\cos \theta} + \frac{1}{\sin \theta}$$

Complex fractions can be simplified in a similar way by multiplying the numerator and denominator by the common denominator.

2. Simplify.

a)  $\frac{\frac{2}{5} + 3}{\frac{1}{2} + \frac{1}{5}}$

b)  $\frac{\frac{\sin \theta}{\cos \theta} + 1}{\frac{1}{\cos \theta} + \sin \theta}$

## Assignment

Simplify each Expression.

1. a)  $\frac{5}{6} + \frac{1}{3}$       b)  $\frac{a}{b} + \frac{c}{ab}$       c)  $\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}$       d)  $\frac{1}{\cos^2 \theta} + \frac{1}{\cos \theta}$
- e)  $\frac{2}{x} + \frac{3}{y}$       f)  $\frac{7}{xy^2} - \frac{15}{x^2 y}$       g)  $\frac{\cos \theta}{\sin \theta} - \frac{1}{\sin^2 \theta}$       h)  $\frac{2}{\sin \theta \cos \theta} - \frac{1}{\cos \theta \sin \theta}$
- i)  $\frac{17a}{bc} + \frac{5b}{ac}$       j)  $\frac{15n^2}{m} + \frac{11n}{m^2}$       k)  $\frac{\sin \theta}{\cos^2 \theta} - \frac{\cos \theta}{\sin \theta}$       l)  $\frac{2\sin \theta}{\cos^2 \theta} - \frac{\sin \theta}{\cos \theta}$
2. a)  $\frac{\frac{2}{2} + 1}{\frac{3}{1} + \frac{1}{3}}$       b)  $\frac{\frac{x}{y} + x}{\frac{y}{x} + y}$       c)  $\frac{\frac{\cos \theta}{\sin \theta} + \sin \theta}{\frac{1}{\sin \theta} + 1}$       d)  $\frac{\cos \theta + \frac{1}{\sin \theta}}{\sin \theta}$
- e)  $\frac{x + \frac{2x}{3}}{6}$       f)  $\frac{6x - \frac{3x}{5}}{3x}$       g)  $\frac{5s - \frac{3s}{4}}{s - \frac{5s}{4}}$       h)  $\frac{\frac{\cos \theta}{\sin \theta} - 1}{1 - \frac{\cos \theta}{\sin \theta}}$
- i)  $\frac{8a + 5 - \frac{3a}{2}}{3a - 7 + \frac{5a}{2}}$       j)  $\frac{2m + \frac{5}{m-3}}{5m - \frac{2}{m-3}}$       k)  $\frac{2s - 5 - \frac{2s^2 - 3s}{s+1}}{3s - 1 - \frac{2s+1}{s+1}}$       l)  $\frac{\frac{\sin \theta}{\cos \theta} + \frac{1}{\cos \theta}}{\frac{1}{\cos \theta} + \frac{\cos \theta}{\sin \theta}}$
- Answers:**
1. a)  $\frac{7}{6}$       b)  $\frac{a^2 + c}{ab}$       c)  $\frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta}$       d)  $\frac{1 + \cos \theta}{\cos^2 \theta}$       e)  $\frac{3x + 2y}{xy}$       f)  $\frac{7x - 15y}{x^2 y^2}$       g)  $\frac{\sin \theta \cos \theta - 1}{\sin^2 \theta}$       h)  $\frac{1}{\sin \theta \cos \theta}$       i)  $\frac{17a^2 + 5b^2}{abc}$       j)  $\frac{n(15mn + 11)}{m^2}$
- k)  $\frac{\sin^2 \theta - \cos^3 \theta}{\sin \theta \cos^2 \theta}$       l)  $\frac{\sin \theta(2 - \cos \theta)}{\cos^2 \theta}$
2. a) 2      b)  $\frac{x^2(1+y)}{y^2(1+x)}$       c)  $\frac{\cos \theta + \sin^2 \theta}{1 + \sin \theta}$       d)  $\frac{\sin \theta \cos \theta + 1}{\sin^2 \theta}$       e)  $\frac{5x}{18}$       f)  $\frac{9}{5}$       g) -17      h) -1      i)  $\frac{13a + 10}{11a - 14}$       j)  $\frac{2m^2 - 6m + 5}{5m^2 - 15m - 2}$       k)  $\frac{-5}{3s^2 - 2}$       l)  $\frac{\sin \theta(\sin \theta + 1)}{\sin \theta + \cos^2 \theta}$