

## 3.1 – Translating Graphs of Functions

In this chapter, we will look at various ways of transforming (changing) graphs of functions.

There are many types of transformations we can make; one of these is **translations**.

A translation is a vertical or horizontal “shift” or “slide” left or right, up or down.

Complete “Construct your Understanding” on p. 162/163 in your worktext.

note:  $y-1=|x|$  is the same as  $y=|x|+1$

**In General:** If  $y=f(x)$ , then:

$y=f(x-h)$  if  $h>0$ , then translate right

$h<0$ , then translate left

$y-k=f(x)$  if  $k>0$ , then translate up

or  $y=f(x)+k$  if  $k<0$ , then translate down

$$y=f(x-3)$$

$$y=f(x+3)$$

$$y=f(x)+3$$

$$y=f(x)-3$$

**Example #1:** Describe each translation to the graph of  $y=f(x)$ .

a)  $y=f(x-3)$

right 3 units

b)  $y=f(x+3)$

left 3 units

c)  $y-3=f(x) \Rightarrow y=f(x)+3$

up 3 units

d)  $y=f(x)-3$

down 3 units

e)  $y+3=f(x+1)$

$$\Rightarrow y=f(x+1)-3$$

left 1 unit

down 3 units

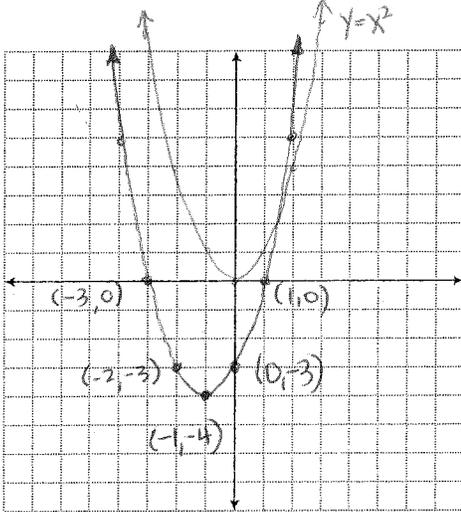
f)  $y=f(x+3)-1$

left 3 units

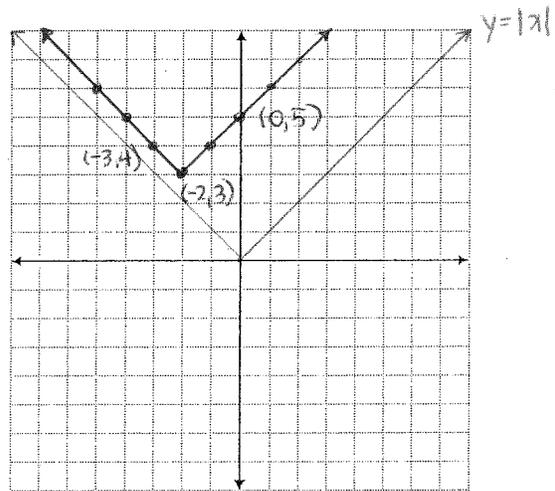
down 1 unit

**Example #2:** Describe the translation(s) for each function. Then, sketch the graph of each function.

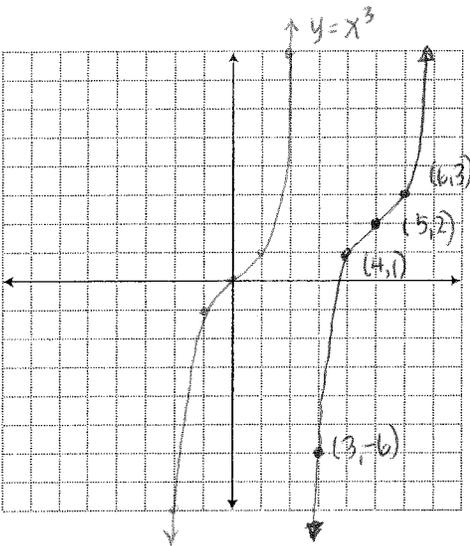
a)  $y = x^2$  and  $y = (x+1)^2 - 4$       left 1  
down 4



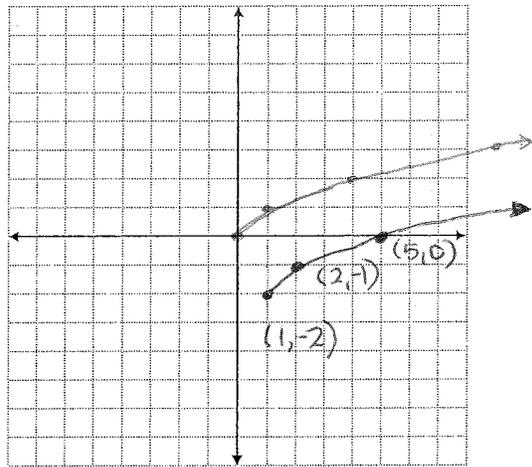
b)  $y = |x|$  and  $y = |x+2| + 3$       left 2  
up 3



c)  $y = x^3$  and  $y = (x-5)^3 + 2$       right 5  
up 2



d)  $y = \sqrt{x}$  and  $y + 2 = \sqrt{x-1} \Rightarrow y = \sqrt{x-1} - 2$       right 1  
down 2



Homework: p. 169 #4 - 16